

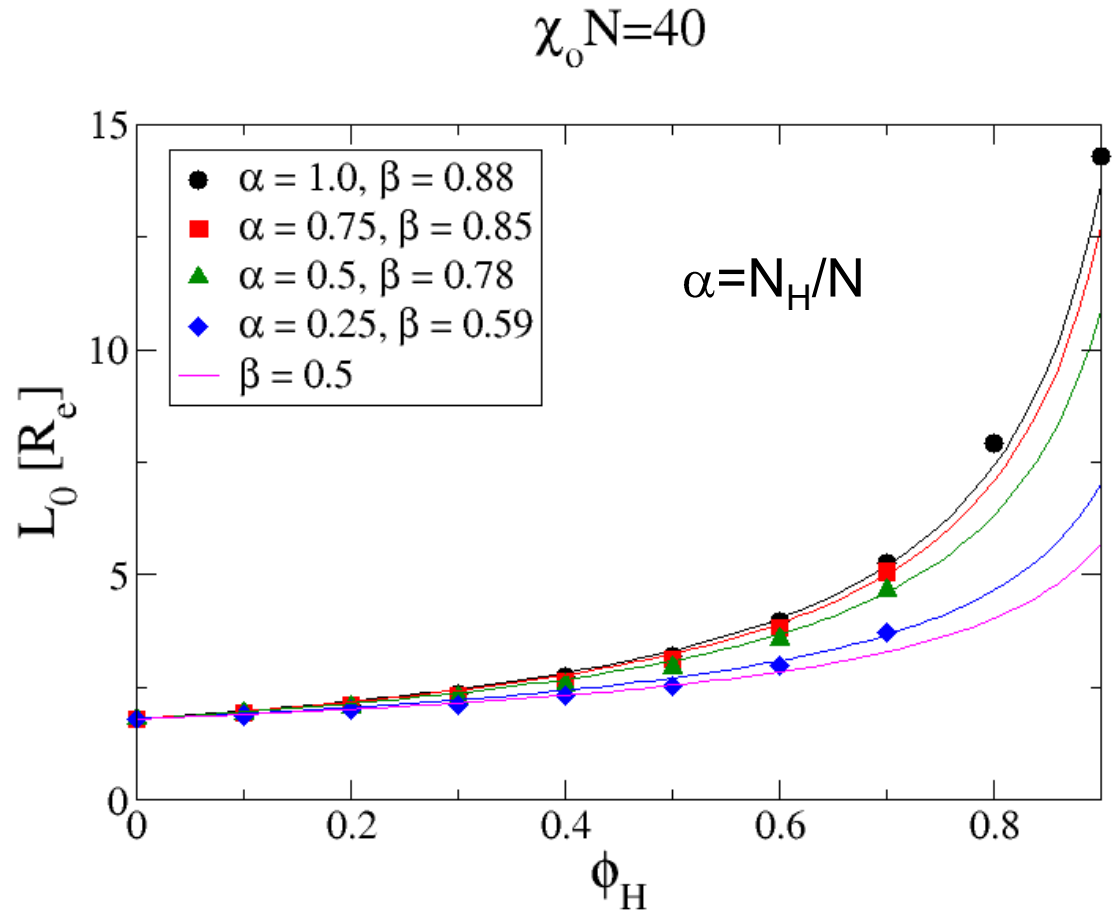
# Control of characteristic period, range of interpolation, and defects through homopolymer addition

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# Ternary Mixtures, Optimal Period

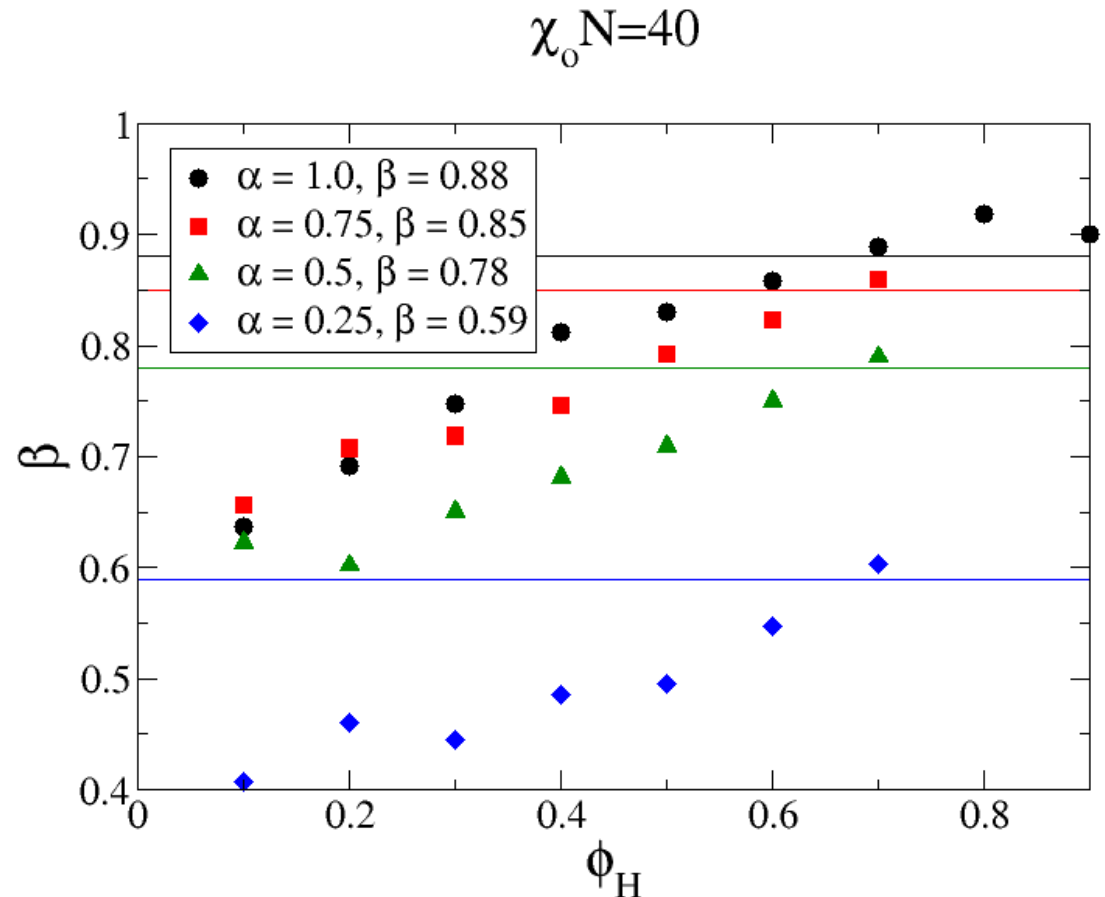
- The diblock copolymer can be swollen by each homopolymer, increasing the period.
- The swelling can be fitted to the equation

$$L_0(\phi_H) = \frac{L_0(\phi_H = 0)}{(1 - \phi_H)^\beta}$$



# Values of $\beta$

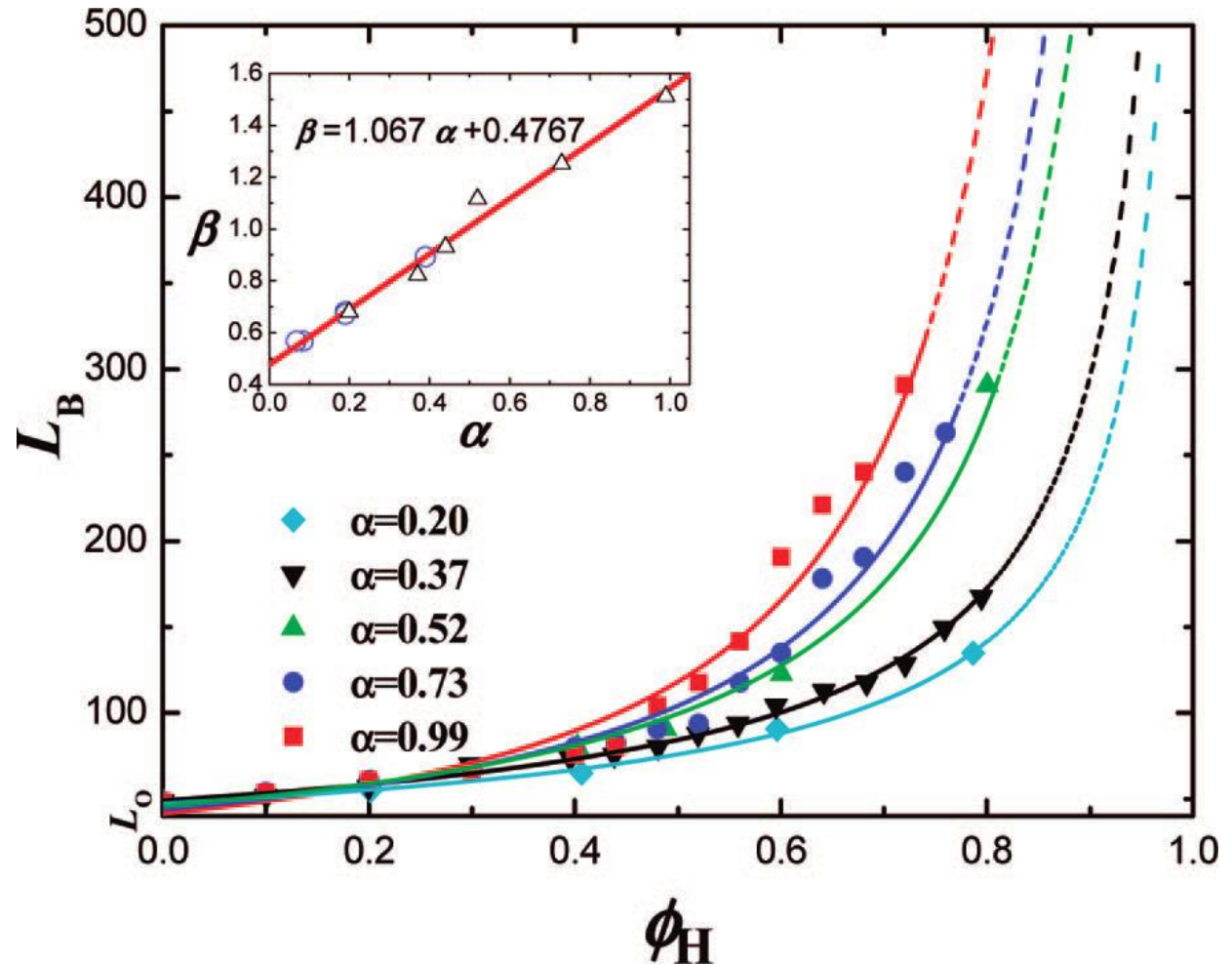
- The value of  $\beta$  drifts as the lamellae become more swollen with homopolymers.
- The curves on the preceding slide use the  $\beta$  values at around  $\phi_H = 0.7$ .



# Experimental Results

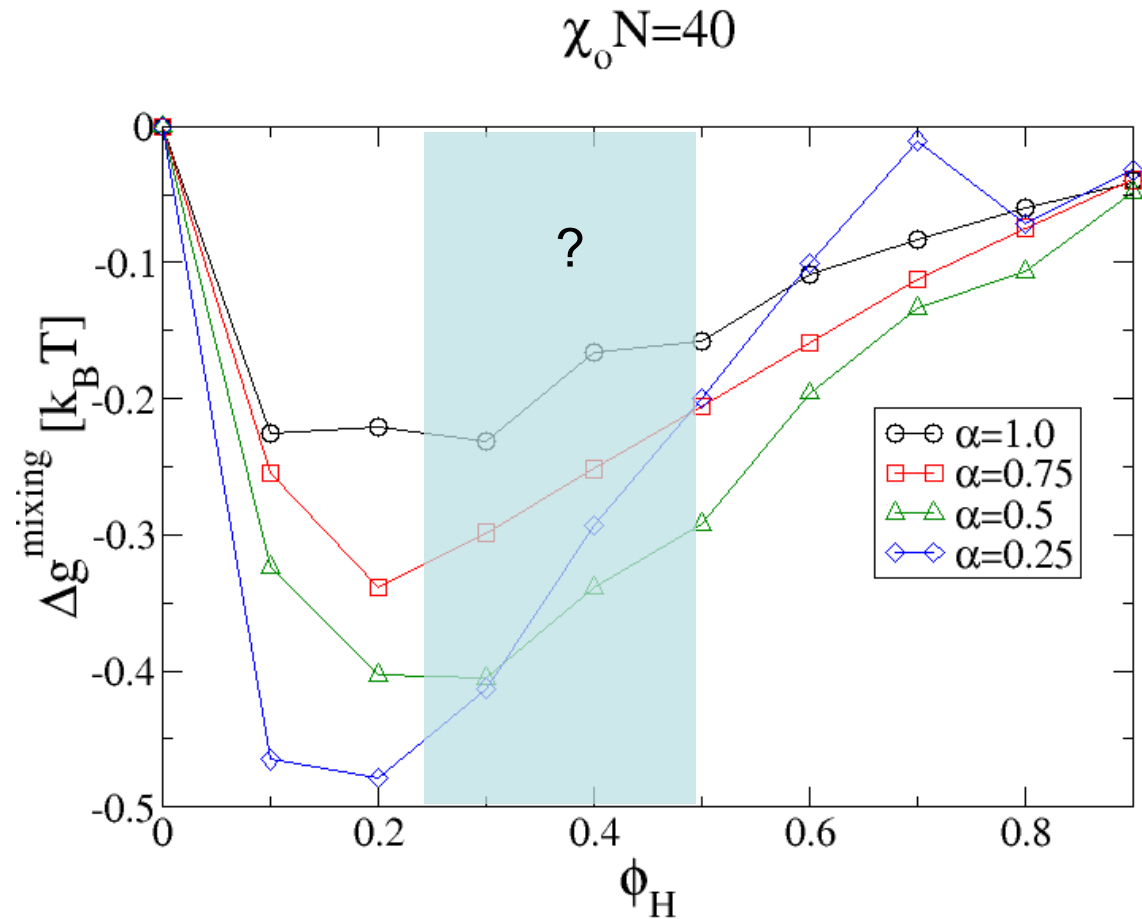
- Experimentally, Guoliang produced larger values of  $\beta$  with a linear dependence in  $\alpha$ .

Liu et. al.  
*Macromolecules*  
**2009**, 42, 3063-3072.



# Energy of Mixing

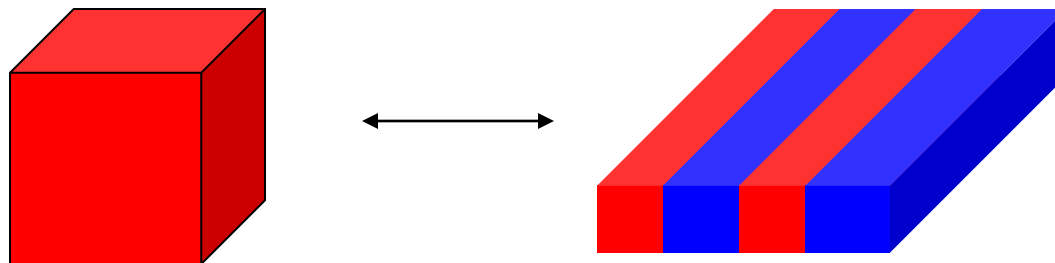
- Free energy of mixing can be determined from Monte Carlo simulations.
- This value, along with interfacial energy and surface energy, can be used to determine where defect free structures are possible.



? First order transition ?

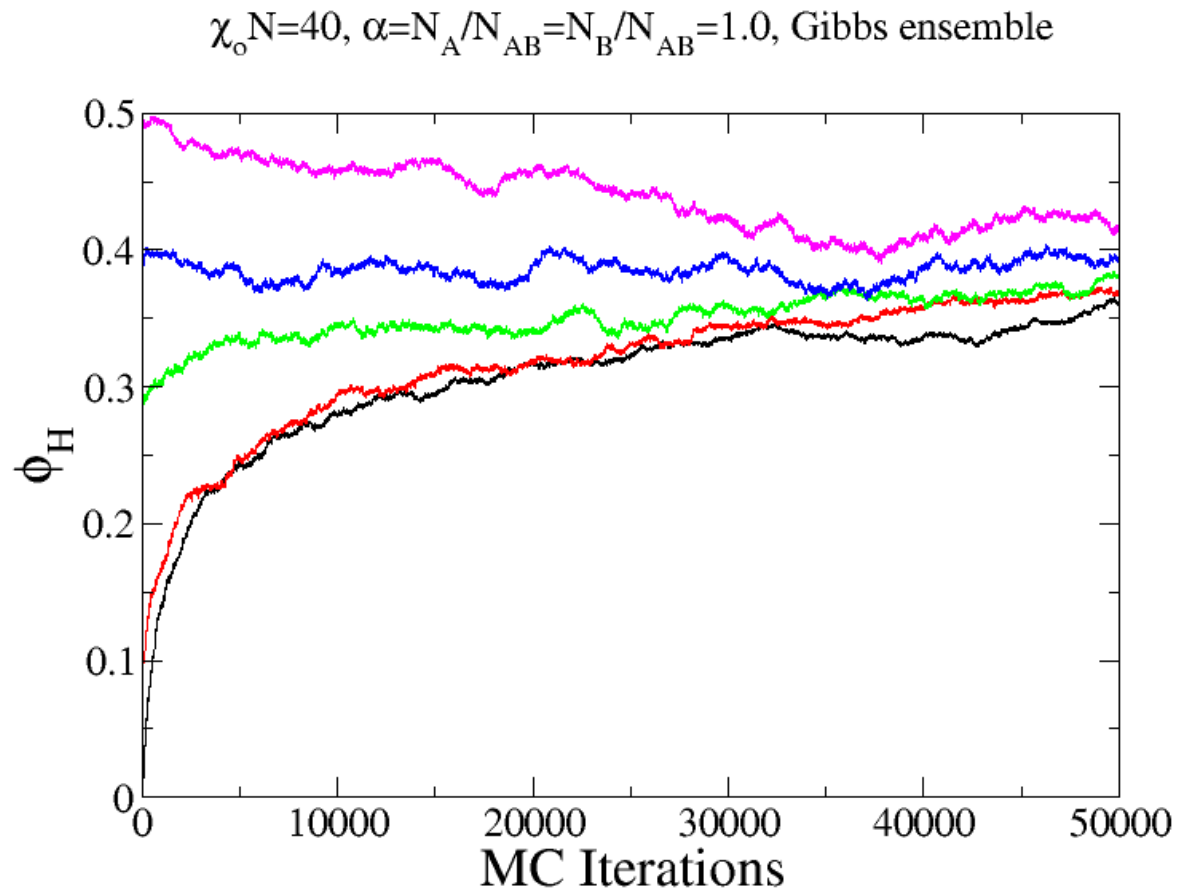
# Optimal Swelling with Gibbs ensemble

- To determine the ideal swelling of the lamellae with homopolymers, a Gibbs ensemble simulation is run.
- One simulation box is lamellae, the other is A-rich. The A-rich simulation box doubles as a B-rich simulation box.



# Optimal Swelling with Gibbs ensemble

- Optimally, the lamellae is swollen with a volume fraction of 0.39 homopolymers when all chains are the same length.



# Comparing chemical potential

- $\mu^{\text{ex}}$  includes the ideal mixing term.

	Lamellar phase	A-rich phase
$\mu^{\text{ex}}$ of copolymer	47.6	47.8
$\mu^{\text{ex}}$ of A polymer	43.3	43.3
$\mu^{\text{ex}}$ of B polymer	43.3	-

- The average volume fraction of copolymers in the A-rich phase is  $2.1 \times 10^{-5}$ . The error in this value may be up to 20%, so it is close enough to  $1.8 \times 10^{-5}$ , the value that gives  $\mu^{\text{ex}}=47.6$ .
- For  $\mu^{\text{ex}}$  of the B homopolymer to match in the 2 phases listed above, the volume fraction in the A-rich phase must be  $8.3 \times 10^{-14}$ . In the Monte Carlo simulation, there is never a B homopolymer in the A-rich phase. The simulation would need to be run over 100 years before a B homopolymer ends up in the A-rich phase.



# Comparing to SCFT

- The ideal MC volume fractions in the A-rich phase (from chemical potential calculations) match closely with the SCFT:

A-rich phase	MC, $\chi_0 N=40$ , $\chi N=32.8$	SCFT, $\chi N=30$	SCFT, $\chi N=35$
$\Phi_{\text{copolymer}}$	$1.8 \cdot 10^{-5}$	$2.7 \cdot 10^{-5}$	$3.0 \cdot 10^{-6}$
$\Phi_{\text{B homopolymer}}$	$8.3 \cdot 10^{-14}$	$9.4 \cdot 10^{-14}$	$6.3 \cdot 10^{-16}$

- The SCFT predicts slightly less homopolymers in the lamellar phase:

Lamellar phase	MC, $\chi_0 N=40$ , $\chi N=32.8$	SCFT, $\chi N=30$	SCFT, $\chi N=35$
$\Phi_{\text{homopolymers}}$	0.39	0.36	0.34

# Optimal Period

- The A-rich phase is almost pure A.
- Thus, the maximally swollen lamellae can be approximated by equating the chemical potential of the homopolymers in the pure phase with that in the lamellae.
- I will verify this trend with Gibbs ensemble, as it is opposite to what is expected.

